A NON-PARAMETRIC STATISTICAL TEST FOR J.R. HICKS' INDUCED INNOVATION HYPOTHESIS

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Abstract

This paper attempts to construct a simple non-parametric statistical test, a combination of a) Student's t-test, b) Wald's F-test and c) calculus for the induced innovation hypothesis published by J. R. Hicks in 1932: "a change in the relative prices of the factors of production is itself a spur to invention, and to invention of a particular kind directed to economizing the use of a factor which has become relatively expensive". The test is performed on parameters estimated from a dynamicized comparatively static economic model constructed by the authors from Lancaster's characteristics consumer behaviour theory and the neoclassical production function with a Gorman-style representative consumer and firm. Estimations are performed on a panel dataset, which comprises 154 countries for the years 1980–2015 (5544 rows) with the help of the General method of Moments (GMM). The paper contributes to the overall economic and historical causes of innovations in economies.

Key words: non-parametric tests, induced innovation, GMM

JEL Code: C23, C51, O30

Introduction

Numerous studies in the history of economics, including the ones in the recent years, such as (Savona & Steinmueller, 2013), (Fabre, 2014), or (Milyaeva & Fedorkevich, 2015), have continuously shown that innovations benefit companies, industries and economies in terms of increasing competitiveness, economic growth and development. There is however little consensus on what are the main causes of innovation. Sir J.R. Hicks, (Hicks, 1964, p. 124), has stated that "a change in the relative prices of the factors of production is itself a spur to invention, and to invention of a particular kind – directed to economizing the use of a factor which has become relatively expensive", which later became the foundation of Hicks' widely discussed Induced Innovation theory. Not even the critics can deny that the theory has been used and in quite a few cases proven empirically. Attempted from the start and followed by ground building paper of William Fellner "Empirical Support for the Theory of Induced Innovation", (Fellner, 1971), there have been several fields in which its endorsement and application was found. The line of research confirming empirically the main hypothesis

included in the theory was originally centred on high wages spurring labour-saving innovation, later agricultural development. More recently the emphasis has shifted towards energy prices and induced innovation in energy-saving technologies. Newell, Jaffe and Stavins, (Newell, Jaffe, & Stavins, 1999), i.a. found the rate of overall innovation independent of energy prices and regulation, however, the direction of innovation was responsive to energy price changes for several products tested by the authors. (Popp, 2002), using patent citations as measure of supply of knowledge found that both energy prices and the quality of existing knowledge have significantly strong positive effects on innovation. Also using patent counts and citation data, (Jang, Du, & al., 2013), confirm that demand and supply factors – including knowledge stocks and crude-oil price – have positive and statistically significant effects on technological biofuel innovations in the United States of America. There is also relatively large number of other correlates to innovation such as inward foreign direct investment (FDI), outward FDI, imports, state guarantees and incentives among many other, as stressed by (Lin & Lin, 2008).

The goal of this paper is to attempt to falsify, in the sense of Popper, Hutchison, Machlup, Lakatos and later Blaug, the Hicks hypothesis by means of a novel statistical test derived from neoclassical and Neokeynesian (orthodox) modelling and corresponding econometric research based on data from official sources in accordance with the instrumentalist principles, formulated by Friedman, Machlup and Musgrave. To do so, we formulate a hypothesis alternative to the Hicks' theory: *"innovation is spurred by an increase in the relative price of one factor of production compensated by a decrease in relative price of another factor of production."* This statement may be used as "sophisticated" falsification of the Induced Innovation Theory¹, for the test of which we employ econometric methodology.

1 Formulating a non-parametric econometric test

To derive a non-parametric econometric test for the Hicks' and alternative hypotheses, we construct an orthodox, i.e. comparative static, model based on Lancaster's characteristics consumer behaviour theory, (Lancaster, 1966)², and on the neoclassical production theory, (Cobb & Douglas, 1928), (Solow, 1956), (Berndt & Christensen, 1973) etc. with Gorman-style

¹ Popper, Hutchison, Lakatos, and Blaug suggest that "sophisticated" falsification is the only criterion of validity of on any scientific theory, which should be rejected if being systematically refuted.

² The "characteristics" consumer behaviour theory, published by Lancaster in 1966, is part of ordinal utility analysis in which quantities of goods/services are replaced with a limited set of characteristics (attributes) so that each good/service is a combination from the set. McFadden, Berry and Pakes offered empirical tests for Lancaster's model.

representative consumer and firm. The following simplifications, in accordance with the instrumentalist *"results justify false assumptions"* create the model's core:

- Two characteristics of goods and services non-innovative and innovative attributes;
- Four factors of production capital-intensive (qualified) labour (*N*), technology complementary to labour (*T*, *T* = $k \cdot N$), natural resources (*A*), and capital (*K*), a linear combination of all inputs, $K = \zeta(N, T, A) = \tilde{\zeta}(N, A)^3$;
- End consumer producer relationships;
- Homogeneity of end consumers and producers;
- Entailed strong(er) competition monopolistic competition or oligopoly on the supply side and perfect or monopsonistic competition on the demand side;
- Absence of extreme solutions and special consumer/company types or relationships as specified in (Němečková, 2013), (Machek & Hnilica, 2015) etc.

Let us suppose a model market or mixed economy of any size⁴ with at least minimum access to natural resource and capital⁵ where *ceteris paribus* (or *ceteris absentibus*) any good and / or service Y_i is a divisible (or at least a mostly divisible) combination of non-innovative and innovative characteristics, the "old attributes" and the "new attributes", depending on four inputs⁶: quantities of qualified labour, z_N , technology complementary to labour (with a fixed N/T relationship)⁷, z_T , natural resources, z_A , and capital, z_K (hereafter omitted from graphs and formal representations of the model because of the exact multicollinearity with the other $z_{k,k\neq K}$ since $K = \tilde{\varsigma}(N, A)$), as well as on the relative prices of $z_{k,k\neq RP}$, $\{z_{RP}\} =$ $\{w_N/w_K, w_N/w_A, w_N/w_T, w_K/w_A, w_K/w_T\}^8$, where $w_{k,k\neq RP}$, are the prices of the inputs.

The formal econometric representation of our model for market equilibrium⁹ in a *multiplicative form*, subsequently simplified with regard to constant (relatively abundant) natural resources, z_A , and the complimentary relationship between technology and qualified

³ In our opinion, such specification is consistent with the neoclassical theory of economics (three factors of production, A, N and K), and reflects the structural changes in economies happening through accumulation of human capital and technology.

⁴ Economy with functioning markets regardless of ownership structure, e.g. U.S., U.K., Germany, France, Japan or China, Russia, Singapore etc.

⁵ Trade and capital restrictions may be present but are not prohibitive in nature, which ensures their relative abundancy at the country level but not at the global level.

⁶ Since productive factor A is considered to be abundant, z_A is left out.

⁷ A requirement of education to employ certain pieces of technology can serve as an example.

⁸ Price of labour is traditionally selected as the most important one.

⁹ Due to the simplified nature of our model, based on Gorman-style representative economic agents and *ceteris paribus* or *ceteris absentibus* assumptions, the terms "general (multimarket) equilibrium" and "market equilibrium" are employed as synonyms.

labour, z_T and $z_N (T = k \cdot N)$, hereafter assumed to be collinear in both volumes (z_N and z_T) and input prices (w_N and w_T)¹⁰, will be the following (for its derivation consult the annex):

$$\sum_{i} \psi_{i} Y_{i}^{*} = AD_{innovations} = AS_{innovations} = \phi(\Pi^{*}, Z^{*}, |\upsilon^{j}, e^{j}, \pi^{j}, c^{j} \dots \text{const}) =$$

$$= \left([\Pi^{\alpha_{0}}] [z_{A} z_{K}^{\beta_{0}} z_{N}^{\beta_{1}} z_{T}^{\beta_{2}}] \left[\left(\frac{W_{N}}{W_{K}} \right)^{\beta_{3}} \left(\frac{W_{N}}{W_{A}} \right)^{\beta_{4}} \left(\frac{W_{N}}{W_{T}} \right)^{\beta_{5}} \left(\frac{W_{K}}{W_{A}} \right)^{\beta_{6}} \left(\frac{W_{K}}{W_{T}} \right)^{\beta_{7}} \right] \right| \dagger \right) = (1)$$

$$\propto \left([\Pi^{\widetilde{\alpha_{0}}}] [z_{A} z_{K}^{\widetilde{\beta_{0}}} z_{N}^{\widetilde{\beta_{1}}}] \left[\left(\frac{W_{N}}{W_{K}} \right)^{\widetilde{\beta_{2}}} \left(\frac{W_{N}}{W_{A}} \right)^{\widetilde{\beta_{3}}} \left(\frac{W_{K}}{W_{A}} \right)^{\widetilde{\beta_{4}}} \right] \varepsilon \right| \dagger \right), \quad \dagger \quad \upsilon^{j}, e^{j}, \pi^{j}, c^{j} \dots \text{const}$$

where $\sum_i \psi_i Y_i^*$ is the equilibrium quantity of innovations in an economy, Π are end prices, Z are inputs, v^j and e^j are utility and expenditure functions, π^j and c^j are profit and cost functions, and each relative input price $\left(\frac{w_b}{w_a}\right)$ is treated as a one, not two variables. Based on equation (1)^{11, 12}, the Hicks' hypothesis and our alternative hypotheses can be formulated as:

$$H_0: \ \forall \ s, \sum_{s=2}^{s=4} \tilde{\beta}_s > 0, \qquad H_1: \ \forall \ s, \sum_{s=2}^{s=4} \tilde{\beta}_s \le 0$$
 (2)

which may be interpreted a custom/made *non-parametric statistical test* (not based purely on individual parameter values but rather on their combinations)¹³, a combination of a) Student's *t*-test, b) Wald's *F*-test¹⁴, and c) arithmetic comparison, non-dependent on any of the model's further modifications, such as eventual exogenous variables.

2 Employed methodology

The nature of our model, applied to panel data, requires the use of the generalized method of moments (GMM), which has the following level and first differences versions, depending on data's time series characteristics (unit roots), after a logarithm transformation of equation (1):

$$E(V - \Gamma \log X | \log X, \log I) = 0,$$

$$E(\Delta V - \Gamma \Delta \log X | \Delta \log X, \Delta \log I) = 0$$
(3)

¹⁰ Proof: If $T = k \cdot N$, then $T \propto N$ and $z_T \propto z_N$, since $T \equiv z_T$ and $N \equiv z_N$. If $w_N = \kappa(N)$ and $w_T = \lambda(T)$, then $w_T = \lambda(k \cdot N) = \tilde{k} \cdot \tilde{\lambda}(N)$ (for a homothetic function $\tilde{k} = k$ and $\tilde{\lambda} = \lambda$), ergo $w_T \propto w_N$.

¹¹ In the detailed model specification, the mark ^{*} indicating equilibrium values of economic variables is omitted.

¹² In this paper, square brackets (crotchets) serve the same purpose as parentheses and are used as their alternative to identify and distinguish between parts of equations.

¹³ The theory of statistics tends to define all non-standard tests as non-parametric which is of course subject to dispute and significantly exceeds the scope of this paper.

¹⁴ Wald *F*-tests are used to estimate statistical significance of groups of parameters, e.g. regression coefficients, in formal models.

where V is the vector of dependent variables, Γ and X are matrices of coefficients and explanatory variables, I is the matrix of eventual exogenous variables. The GMM weights in this paper are calculated, according to the standard rule-of-thumb formula:

$$W = (\text{number of observations}) * (\log X, \log I)' (\log X, \log I),$$
(4)

 $\widetilde{W} = (\text{number of observations}) * (\Delta \log X, \Delta \log I)'(\Delta \log X, \Delta \log I)$

To choose between the level and first difference versions of the econometric model, we employ the augmented Dickey and Fuller, ADF, test and the Kwiatkowski–Phillips–Schmidt–Shin, KPSS, tests with constant and a time trend. In this paper, we use Choi's meta-analysis, where the overall (composite) p-value is estimated from the p-values of ADF tests and p-value range estimations of KPSS tests for individual cross-sections.¹⁵

3 Data

Data for all variables were retrieved from official sources, specifically, from the World Intellectual Property Organization (WIPO), Penn World Tables 9.0 (University of Groningen), the International Monetary Fund (IMF), International Labour Organisation (ILO), the World Bank Group (WB), United Nations Development Programme (UNDP), as well as from the United Nations Conference on Trade and Development (UNCTAD). A detailed overview of the panel dataset, which comprises 154 countries for years 1980–2015 (5544 rows and ca. 7.1% missing observations), is provided in Table 1. The following modifications were performed in the panel dataset before performing the GMM estimation: a) missing values were interpolated by arithmetic and geometric means and extrapolated with the help of repeating border values; b) for the calculation of w_{NK} and w_{NA} , real wages were logaritmized in order to smooth the effects of monetary policies and inflation in specific years. We also adopted the methodology of the Global Innovation Index (GII), the leading yearbook on innovation in the world, to add several exogenous variables into the dataset.

Tab. 1: Panel dataset overview

	Description			Unit / Formula					
трр	Intellectual	property	protection,	Number	of	patent,	utility	design	and
	number of applications			utility model applications					

¹⁵ There is no single methodology for verifying the presence of unit roots in time series and panel datasets. Hence, it is always advisable to use more than one test. ADF and KPSS have different logic: the H_0 hypothesis of the ADF test is the presence of a unit root in the time series, whilst the H_0 of the KPSS test is the time series' stationarity. Choi meta-tests may also not be the only approach for panel unit root testing but we choose them over the 100% pooled Levin-Lin-Chu and Harris-Tzavalis tests.

Р	Total prices, index	Consumer price index, $2005 = 100$			
zA	Natural resources	constant			
		Obtained as a product of million persons			
zQN	Qualified labour million persons	employed and Penn World Table 9.0			
	with human capital	Index of human capital per person,			
	with numan capital	based on years of schooling and returns			
		to education (the <i>hc</i> variable).			
zK	Capital stock	Stock of capital, constant prices of 2011			
ZN	Cupital Stock	\$US			
wNK	Prices of capital / prices of	Real interest rate / real wage index,			
	qualified labour	2005 = 100			
	Prices of qualified labour / prices	Real wage / International Monetary			
wNA	of commodities	Fund's commodity price index,			
	or commodities	2005 = 100			
		Real interest rate / International			
wKA	Prices of capital / prices of	Monetary Fund's commodity price			
WKA	commodities	index,			
		2005 = 100			

Exogenous variables:

INST	Quality of institutions, index	Transparency international & Others Corruption Perception Index, 0–10			
HCR	Length of schooling and life expectancy, index	Obtained as a residual of ordinary least squares (OLS) regression of human development index into on an improvised gross national index per capita in purchasing power parity. Non- collinear with zQN, according to the de- trended correlation coefficient.			
INFR	Quality of infrastructure, share	Gross capital formation, current prices, share in GDP			
MBSex	Market and business sophistication indicator - part 1, share	Exports of goods and services, share in GDP			

	Market and business sophistication	Foreign direct investment net outflow,
	indicator - part 2, share	share in GDP
MBSfdinOUT		

Dummy variables:

time	time trend, added with the help of z_0 parameter onto the model
unit	Country-specific effects, added with the help of z_1 parameter onto the model
Source: authors	·

Source: authors.

3 Results

Preliminary estimations show heterogeneous non-stationarity of time series inside the abovedescribed panel variables, hence, we recur to their stationarization via log-differences (ld_), which are employed in the model, as shown in Table 2 (all missing observations were omitted in calculation).

Tab. 2: Iterated GMM estimation in gretl

CIMI CITCCIIOI	1 = 15339.47014	100 (ste	eplength =	1.31072e-	-12)	
Parameters:	-0.21583 -0.2	18427	-0.031300	-0.010525	0.697	13 0.39677
	0.019911 -0.0	030871	2.0792e-05	1.4138e-0)5	
Gradients:	0.47521 -0.3	13370	-1.2806	0.98862	0.015	370 -0.14961
	-1.6616 -1	.4812	30.509	56.112 (no	orm 1.81e-	01)
Tolerance = 1 Function eval Evaluations c Model 7: Iter e = ld_IPP(-1 - b1 * ld_zQN z0 * time - z	81899e-12 .uations: 19 of gradient: 1 cated GMM, usir) - w0 * ld_IP N(-1) - b2 * 1 c1 * unit	ng obser P(-2) - d_zK(-1	wations 3- w1 * ld_I) - b3 * 1	-1950 (n = PP - a0 * ld_wNK(-1	= 1948) ld_P(-1)) - b4 *) - b0 * const 1d_wNA(-1) -
	estimate	std. e	error	Z	p-value	
 w0	estimate 	std. e	error 	z 	p-value	***
 w0 w1	estimate -0.215826 -0.184266	std. e 0.0664 0.0679	267 -3	z 3.249 2.713	p-value 0.0012 0.0067	* * *
 w0 w1 a0	estimate -0.215826 -0.184266 -0.0313002	std. e 0.0664 0.0679 0.0198	error 267 -3 310 -2 3508 -1	z 3.249 2.713 577	p-value 0.0012 0.0067 0.1148	* * *
 w0 w1 a0 b0	estimate -0.215826 -0.184266 -0.0313002 -0.0105247	std. e 0.0664 0.0679 0.0198 0.0233	error 2267 -3 310 -2 3508 -1 3966 -0	z 3.249 2.713 .577).4498	p-value 0.0012 0.0067 0.1148 0.6528	* * *
w0 w1 a0 b0 b1	estimate -0.215826 -0.184266 -0.0313002 -0.0105247 0.697130	std. e 0.0664 0.0679 0.0198 0.0233 0.3259	error 2267 -3 3310 -2 3508 -1 3966 -0 227 2	z 3.249 2.713 577 0.4498 2.139	p-value 0.0012 0.0067 0.1148 0.6528 0.0324	* * *
w0 w1 a0 b0 b1 b2	estimate -0.215826 -0.184266 -0.0313002 -0.0105247 0.697130 0.396770	std. e 0.0664 0.0679 0.0198 0.0233 0.3259 0.1593	error 267 -3 3310 -2 3508 -1 3966 -0 27 2 380 2	z 3.249 2.713 577 0.4498 2.139 2.489	p-value 0.0012 0.0067 0.1148 0.6528 0.0324 0.0128	* * * * * * * *
w0 w1 a0 b0 b1 b2 b3	estimate -0.215826 -0.184266 -0.0313002 -0.0105247 0.697130 0.396770 0.0199109	std. e 0.0664 0.0679 0.0198 0.0233 0.3259 0.1593 0.0403	error 2267 -3 3310 -2 3508 -1 3966 -0 227 2 380 2 3584 0	z 3.249 2.713 .577 0.4498 2.139 2.489 0.4934	p-value 0.0012 0.0067 0.1148 0.6528 0.0324 0.0128 0.6218	* * * * * * * *
w0 w1 a0 b0 b1 b2 b3 b4	estimate -0.215826 -0.184266 -0.0313002 -0.0105247 0.697130 0.396770 0.0199109 -0.0308705	std. e 0.0664 0.0679 0.0198 0.0233 0.3259 0.1593 0.0403 0.0403	error 267 -3 310 -2 3508 -1 3966 -0 227 2 380 2 3584 0 939 -0	z 3.249 2.713 .577 0.4498 2.139 2.489 0.4934 0.8322	p-value 0.0012 0.0067 0.1148 0.6528 0.0324 0.0128 0.6218 0.4053	* * * * * * * *
w0 w1 a0 b0 b1 b2 b3 b4 z0	estimate -0.215826 -0.184266 -0.0313002 -0.0105247 0.697130 0.396770 0.0199109 -0.0308705 2.07917e-05	std. e 0.0664 0.0679 0.0198 0.0233 0.3259 0.1593 0.0403 0.0370 0.0008	error 267 -3 310 -2 508 -1 3966 -0 27 2 880 2 3584 0 939 -0 316102 0	z 3.249 2.713 .577 0.4498 2.139 2.489 0.4934 0.8322 0.02548	p-value 0.0012 0.0067 0.1148 0.6528 0.0324 0.0128 0.6218 0.4053 0.9797	* * * * * * * *
w0 w1 a0 b0 b1 b2 b3 b4 z0 z1	estimate -0.215826 -0.184266 -0.0313002 -0.0105247 0.697130 0.396770 0.0199109 -0.0308705 2.07917e-05 1.41383e-05	std. e 0.0664 0.0679 0.0198 0.0233 0.3259 0.1593 0.0403 0.0403 0.0370 0.0008	267 -3 310 -2 3508 -1 3966 -0 27 2 380 2 380 2 380 2 380 -0 310 27 2 380 -0 310 27 2 380 -0 380 -0 380 -0 27 2 380 -0 27 2 380 -0 285 -0 380 -0 293 -0 380 -0 293 -0 380 -0 293 -0 203 -0	z 3.249 2.713 577 0.4498 2.139 2.489 0.4934 0.8322 0.02548 0.06830	p-value 0.0012 0.0067 0.1148 0.6528 0.0324 0.0128 0.6218 0.4053 0.9797 0.9455	* * * * * * *

Source: self-prepared

The only significant parameters of the model, according to the iterated GMM estimation, the quality of which was confirmed by Sargan-Hansen J-test, are w0, w1, b1 and b2. Parameters of relative input prices b3 and b4, crucial for this paper, have been found statistically non-significant at all 1%, 5% and 10% probability levels, which proves the alternative hypothesis H_1 and reject H_0 in our non parametric test. Parameter b5 and variable wKA were omitted from the model because of the exact collinearity.

Conclusion

No significant disagreement exists about the notion that innovations are beneficial to individual companies as well as to economic development of entire economies. There is however little consensus on what is the cause of innovation. The Hicks hypothesis of "induced innovation" is a classic example of a long-standing innovation theory as much as of many inconclusive discussions. In our paper, we have attempted to falsify it by offering a hypothesis alternative to the Hicks' theory, developed a theoretical model to justify it and constructed and performed an econometric test of the model. Our suggested way of putting the hypothesis to scrutiny by data represents a novel non-parametric (non-standard and not purely parameter value based) statistical test based on combinations of parameter values from an economic model and arithmetic operations, which creates the first (methodological) value added of our research. We agree with Hicks in principle that an increase in the relative price of a factor of production can carry a motivation to replace it through innovation, however, simple increase of price of one (or several) factors might not be enough. More to the point, inflating prices of input(s) can be debilitating as company or industry loses competitiveness and diminishes. Our key point thus is that the increase in relative price of one factor mandate relatively low price level of other factor(s) of production as a compensation of cost for companies for the innovations to take place. Our econometrical results haven't backed the Hicks' hypothesis but rather our alternative one, which forms the second (practical) value added of our research.

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Annex: Formal derivation of the model

Under the condition of $\forall Y_i \ge 0$, *Innovative* attributes $= \sum_i \psi_i Y_i$, *Non-innovative* attributes $= \sum_i \chi_i Y_i$, where *i* is the number of good/service *Y*, and ψ_i and χ_i are the shares of the two characteristics in each Y_i .

Demand side:

$$d^{j} \propto \operatorname{NP}C_{d}^{j}: \nu(i) = \upsilon^{j}(i, \Pi, y) = \max_{U} U\left(\sum_{i} \psi_{i} Y_{i}, \sum_{i} \chi_{i} Y_{i}\right) \quad \text{s.t.} \quad \sum_{i} p_{i} Y_{i} \leq y$$

where *j* is the end consumer, NPC_d^j is the "novelty/innovation product curve", from which the individual demand for innovations is derived, and p_i is the price of of Y_i , is equivalent to:

$$d^{j} \propto \text{NPC}_{d}^{j}: \eta(i) = e^{j}(i, \Pi, \overline{U}) = \min_{\forall Y_{i}} \sum_{i} p_{i} Y_{i} \quad \text{s.t.} \quad U\left(\sum_{i} \psi_{i} Y_{i}, \sum_{i} \chi_{i} Y_{i}\right) \geq \overline{U}$$

ergo

$$d_{innovations}^{j} = \sum_{i} \psi_{i} Y_{i} = \xi \left(e^{j} \left(i, \Pi, \upsilon^{j}(i, \Pi, y) \right) \right) = f^{j}(\Pi) + g(\Pi) \cdot \tilde{\upsilon}^{j}(i, \Pi, y) + h^{j}$$

and

$$AD_{innovations} = \sum_{j} d^{j}_{innovations} = \sum_{j} \sum_{i} \psi_{i} Y_{i} = \sum_{j} \xi \left(e^{j} \left(i, \Pi, \upsilon^{j} (i, \Pi, y) \right) \right) = f(\Pi) + g(\Pi) \cdot \tilde{\upsilon}(i, \Pi, y) + h$$

ergo, under constant v^j and e^j ,

 $AD_{innovation} = \lambda(\Pi | \upsilon^{j}, e^{j} ... const)$

Supply side:

$$s^{j} \propto NPC_{s}^{j}$$
: $\rho(i) = \pi^{j}(i, \Pi, IC) = \max_{\pi} \sum_{i} p_{i}Y_{i} - IC \quad \text{s.t.} \quad \forall \ z_{k,k \neq RP} \sum_{k} w_{k,i} z_{k} \leq IC$

where *j* is the producer, *NPC* is the "novelty/innovation product curve" from which the individual supply of innovations is derived, *k* is the input, and w_k is the absolute price of the input $z_{k,k\neq RP} \in Z$, is equivalent to:

$$s^{j} \propto NPC_{s}^{j}: \phi(i) = c^{j}(i, \mathbb{Z}, \overline{\pi}) = \min_{\forall Z_{k,k \neq RP}} \sum_{k} w_{k} Z_{k} \quad \text{s.t.} \quad \sum_{i} p_{i} Y_{i} - IC \geq \overline{\pi}$$

ergo

$$s_{\text{innovations}}^{j} = \sum_{i} \psi_{i} Y_{i} = \zeta \left(c^{j} \left(i, Z, \pi^{j} (i, \Pi, IC) \right) \right) = l^{j} (Z) + m(Z) \cdot \tilde{\pi}^{j} (i, \Pi, IC) + n^{j}$$

and

$$AS_{\text{innovations}} = \sum_{j} s_{\text{innovations}}^{j} = \sum_{j} \sum_{i} \psi_{i} Y_{i} = \sum_{j} \zeta \left(c^{j} \left(i, Z, \pi^{j} (i, \Pi, IC) \right) \right) =$$
$$= I(Z) + m(Z) \cdot \widetilde{\pi}(i, \Pi, IC) + n$$

ergo, under constant π^{j} and c^{j} ,

AS_{innovation} = $\mu(Z, \Pi \mid \pi^{j}, c^{j} ... const), Z = \{w_{N}/w_{K}, w_{N}/w_{A}, w_{N}/w_{T}, w_{K}/w_{A}, w_{K}/w_{T}\}$

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